

## How to do things with words 2: speech acts and mutual joint belief

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- 1 Role and interpretation of 'agreement'
- 2 Logic of mutual joint belief (Stalnaker 2002, Fagin & al. 1995)
- 3 Truckenbrodt 2008: self-verification for social act propositions
- 4 Reconsidering social facts
- 5 Conclusion

# Outline

- 1 Role and interpretation of 'agreement'
- 2 Logic of mutual joint belief (Stalnaker 2002, Fagin & al. 1995)
- 3 Truckenbrodt 2008: self-verification for social act propositions
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- 5 Conclusion

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- take serious: connection  $[[\textit{sentence}]] \leftrightarrow \text{SPEECH ACT}$
- add: contextual factor of mutual joint belief

# Truth-conditions and ASSERTIONS

(1) *Regine is in Norway.* ASSERTION

(2) *I promise you to call Regine tonight.* PROMISE

- declarative clauses aren't ASSERTIONS, they denote propositions:

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- truth conditional semantics has a natural link to ASSERTIONS
- ASSERTIONS (minimally): S provides information to reduce epistemic uncertainty  
 S does so by enriching **joint information** (vs. anonymous note)

# A model of joint information: Stalnaker

- doxastic uncertainty is modelled by the set of possible worlds  $w'$  that given a body of beliefs held in  $w$  cannot be ruled out as candidates for  $w$  (doxastic alternatives)

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**Common belief**  $CB_{A,w}$ : A proposition  $\phi$  is common belief of a group of believers  $A$  in  $w$  (short:  $CB_{A,w}(\phi)$ ) iff all in the group believe that  $\phi$ , all believe that all believe it, all believe that all believe that all believe it, ...

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- context set CS intersected with proposition described by *declarative sentence*:
$$CS_{new} := \{w \mid w \in CS_{old} \wedge \llbracket decl.sentence \rrbracket(w) = 1\}$$
- side-remark: a speech act that amounts to adding a proposition to the Common Ground need not be an ASSERTION

# Non-assertive acts and propositions: Truckenbrodt 2008

Truckenbrodt assumes that some propositions are inherently self-verifying (under contextual conditions) thanks to their lexical semantics:

- (3) For performative  $p$  and contextual conditions  $C$ :
- $$\forall w, x, y[\text{say}(w)(x, y, p) \wedge C(w)(x, y, p)] \rightarrow p(w)]$$

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Starting point is Searle's (1995) distinction of:

- **brute facts** ordinary facts about the world
- **institutional facts** constituted by agreement (10\$-bill)

Searle extends this to language:

- (4) *The meeting is adjourned.*

▶ How to model 'agreement'?

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**Claim 1:** The content of a performative sentence  $S$  can be paraphrased as a fact about mutually joint agreement:  
there is a proposition  $p$  s.t.  $\llbracket S \rrbracket \Leftrightarrow CB(p)$ .

**Claim 2:** such sentences are self-verifying if they are used to update the Common Ground.

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- $a$ 's doxastic alternatives in  $w$ :  $\{w' \mid wR_a w'\}$
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② If  $a$  believes  $\phi$ , she believes that she believes  $\phi$  (positive introspection:  $B_{a,w}(\phi)$  entails  $B_{a,w}(B_a(\phi))$ ).

... **transitive**:  $\forall w \forall w' \forall w'' [wRw' \wedge w'Rw'' \rightarrow wRw'']$ .

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- ③ If  $a$  does not believe  $\phi$ , then she believes that she does not believe  $\phi$  (negative introspection:  $\neg B_{a,w}(\phi)$  entails  $B_{a,w}(\neg B_a(\phi))$ ).

... **euclidian**:  $\forall w \forall w' \forall w'' [wRw' \wedge wRw'' \rightarrow w'Rw'']$ .



# Positive introspection

$B_{a,w}(\phi)$  entails  $B_{a,w}(B_a(\phi))$ .

Follows from **transitivity**:  $\forall w \forall w' \forall w'' [wRw' \wedge w'Rw'' \rightarrow wRw'']$ .

Proof (indirect):

$B_{a,w}(\phi)$ . By definition,  $\forall w' [wR_a w' \rightarrow w' \in \phi]$ .

Assume not  $B_{a,w}(B_a(\phi))$ . Then not

$\forall w' [wR_a w' \rightarrow \forall w'' [w'R_a w'' \rightarrow w'' \in \phi]]$ . Hence,

$\exists w' \exists w'' [wR_a w' \wedge wR_a w'' \wedge w'' \notin \phi]$ . By transitivity,  $wR_a w''$ . So, we derive  $B_{a,w}(\phi)$  which contradicts the given statement.

Therefore, it must be that  $B_{a,w}(B_a(\phi))$ .

*q.e.d.*

# Negative introspection

$\neg B_{a,w}(\phi)$  entails  $B_{a,w}(\neg B_a(\phi))$ .

Follows from **euclidity**:  $\forall w \forall w' \forall w'' [wRw' \wedge wRw'' \rightarrow w'Rw'']$ .

Proof of negative introspection: (indirect)

$\neg B_{a,w}(\phi)$ . Hence, there is a world  $w_1$ , such that  $wR_a w_1$  and  $w_1 \notin \phi$ .

Assume not  $B_{a,w}(\neg B_a(\phi))$ . That is,

$\neg \forall w_2 [wR_a w_2 \rightarrow [\neg \forall w_3 [w_2 R_a w_3 \rightarrow w_3 \in \phi]]]$ . Hence, there is a  $w_2$  s.t.  $wR_a w_2$  and  $\forall w_3 [w_2 R_a w_3 \rightarrow w_3 \in \phi]$ ; by euclidity, for any world  $w_1$  s.t.  $wR_a w_1$  also  $w_2 R_a w_1$ . So, there cannot be a world  $w_1$ , such that  $wR_a w_1$  and  $w_1 \notin \phi$ . Thus we obtain  $B_{a,w}(\phi)$  which contradicts the given statement.

Therefore, it must be that  $B_{a,w}(\neg B_a(\phi))$ . *q.e.d.*

# Belief relations are pseudo-reflexive

**reflexive:**  $\forall w[wRw]$ .

Belief relations need not be reflexive, as subjects can have wrong beliefs (can exclude their own world).

Belief relations are **pseudo-reflexive:**  $\forall w\forall w'[wRw' \rightarrow w'Rw']$

Proof:  $R$  is euclidian, hence for any  $wRw'$ ,  $w'Rw'$ . *q.e.d.*

# Common belief CB

Common Belief in  $w$  of a group  $A$ :

$CB_{A,w}(\phi)$  iff  $\forall w'[wR_A w' \rightarrow w' \in \phi]$ , where  $R_A = (\bigcup_{a \in A} R_a)^+$   
(transitive closure of the union of all participant's belief relations).

Schiffer 1972, Stalnaker 2002

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- $CB_{A,w}(\phi)$  entails  $CB_{A,w}(CB_A \phi)$ . Positive Introspection.

Proof: by transitivity, see proof for individual belief above.

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Proof: by transitivity, see proof for individual belief above.
- Pseudo-reflexivity holds (to show).
- Negative Introspection does not hold. (The relation need not be euclidian.)  
 ▶ There are cases of unawaredly unshared belief:  
 $\neg CB_{A,w}(\phi)$  but not  $CB_{A,w}(\neg CB_A \phi)$ .



## Example: unawarely unshared belief

Group:  $A = \{a, b\}$ .  $p = \lambda w$ . there is time pressure in  $w$ .

Assume:  $\neg CB_{A,w}(p)$ .

Hence,  $\exists w' [wR_A w' \wedge \neg p(w')]$ , so there is some sequence  $wR_{i_1} w_1 \dots R_{i_{n-1}} w'$  with  $i_j \in \{a, b\}$  for  $1 \leq j \leq n$  and  $\neg p(w')$ .

E.g. for all  $w_1$  where  $wR_a w_1$ :

- $\neg p(w_1)$ . (a believes there is no time pressure)
- $\forall w' [w_1 R_b w' \rightarrow p(w')]$   
(a believes that b believes that there is time pressure).
- $\forall w'' \forall w_2 [w_1 R_b w_2 \wedge w_2 R_a w'' \rightarrow p(w'')]$   
(a believes b believes a believes there is time pressure).
- And so on for all *ab*-series.

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So, not  $\neg B_a(p)$ , by definition of  $CB_A$ ,  $\neg CB_A(p)$  (proof cf. script);  
but a believes that b believes that  $CB_A(p)$ .

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But:  $b$  believes there is time pressure, and  $b$  believes that  $a$  believes that there is time pressure and that all  $ab$ -series support that there is time pressure:

$$B_{b,w}(CB_A p)$$

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$$B_{b,w}(CB_A p)$$

$R_A$  is not euclidian - worlds  $w_1$  (accessible to  $a$ ) and  $w_3$  (accessible to  $b$ ) need not see each other. Fits our intuitions about common belief.

# Cancellability of multiple CB

Theorem on Common Belief in  $w$  of a group  $A$ :

$$CB_{A,w}(\phi) \Leftrightarrow CB_{A,w}(CB_A\phi).$$

Stalnaker 2002 sans proof; Truckenbrodt 2008 for a proof by structural induction

$\Rightarrow$ : by Positive Introspection, ✓;  $\Leftarrow$ :  show.

*Lemma*: Mutual joint belief is quasi-reflexive.

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*Lemma*: Mutual joint belief is quasi-reflexive.

- Proof: Assume  $wR_A v$ . Then, either (i) there is a single step s.t. for some  $a \in A$ ,  $wR_a v$ . Since  $R_a$  is quasi-reflexive,  $vR_A v$ . Or (ii), there are  $z_1, \dots, z_n$  for  $n \geq 1$  s.t.  $wR_{i_1} z_1 \dots z_n R_{i_{n+1}} v$  where  $i_r \in A$  for  $1 \leq r \leq n+1$ . So,  $R_{i_{n+1}} = R_a$  for some  $a \in A$ . As  $R_a$  is quasi-reflexive,  $vR_{i_{n+1}} v$ , hence  $vR_A v$ . *q.e.d.*

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*Lemma*: Mutual joint belief is quasi-reflexive.

Proof  $\Leftarrow$ : If  $CB_{A,w}(CB_A\phi)$ , then  $\forall v[wR_{Av} \rightarrow [\forall u[uR_{Av} \rightarrow u \in \phi]]]$ . From  $wR_{Av}$ , by quasi-reflexivity, it follows that  $vR_{Av}$ . Therefore,  $\forall v[wR_{Av} \rightarrow v\phi]$ . So,  $CB_{A,w}(\phi)$ . *q.e.d.*

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# Social facts in terms of lexical paraphrases: Truckenbrodt 2008

The content of any performative sentence  $S$  can be paraphrased as a fact about mutually joint agreement:  $\llbracket S \rrbracket \Leftrightarrow CB(p)$ .

Agreement is equivalent to fact:  $CB(\llbracket S \rrbracket)$

$\Leftrightarrow CB(CB(p))$

lexical equivalence

$\Leftrightarrow CB(p)$

theorem about  $CB$ , Stalnaker 2002, fn. 7

$\Leftrightarrow \llbracket S \rrbracket$  is true.

lexical equivalence, backward.

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The content of any performative sentence  $S$  can be paraphrased as a fact about mutually joint agreement:  $\llbracket S \rrbracket \Leftrightarrow CB(p)$ .

Agreement is equivalent to fact:  $CB(\llbracket S \rrbracket)$

$\Leftrightarrow CB(CB(p))$

lexical equivalence

$\Leftrightarrow CB(p)$

theorem about  $CB$ , Stalnaker 2002, fn. 7

$\Leftrightarrow \llbracket S \rrbracket$  is true.

lexical equivalence, backward.

Example:  $\llbracket own \rrbracket(x)(y) \Leftrightarrow$

$CB_{A,w}(\lambda w'. \forall z \in A : use(z, y)(w')) \rightarrow$

$[\text{authorize}(x, \lambda w''. use(z, y)(w''))(w') \vee \text{sth-wrong}(w')]$

$CB_{A,w}(\lambda w'. own(x, y)(w'))$  iff  $own(x, y)(w')$ .

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- 1 cancellability of  $CB$  (✓)

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② properties of the particular account ➡ check!

# Update

Truckenbrodt (2008):

- (5) Stalnaker 1978: In an ASSERTION,  $p$  is added to the common ground of  $S$  and  $A$ , unless  $A$  objects. [his 17]
- (6) By using a declarative clause ([*-wh,-imp*]), indicative verbal mood, falling intonation) with proposition  $p$ , a speaker adds  $p$  to the Common Ground if the addressee does not object. (Formally: **the context set is intersected** with  $p$ .) [his 19]

Define update of  $CB_A$  with  $p$ : Eckardt (draft, p.8)

$$(7) \quad R_a \oplus p := \{ \langle w, w' \rangle \mid \langle w, w' \rangle \in R_a \wedge p(w') \}$$

two possibilities:

- (8) a.  $R_A \oplus p := (\bigcup_{a \in A} (R_a \oplus p))^+$  local
- b.  $R_A \oplus p := \{ \langle w, w' \rangle \mid \langle w, w' \rangle \in R_A \wedge p(w') \}$  global

# Worries about lexical equivalence: biconditional

- equivalence between agreement and fact:

$$\begin{aligned}
 & \llbracket \text{own} \rrbracket(x)(y) \Leftrightarrow \\
 & CB_{A,w}(\lambda w'. \forall z \in A : \text{use}(z, y)(w') \rightarrow \\
 & \quad [\text{authorize}(x, \lambda w''. \text{use}(z, y)(w''))(w') \vee \text{sth-wrong}(w')]) \\
 & \Rightarrow \text{no uncertainty among the relevant people.}
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- but:

(9)    A: *Is this pencil mine or yours?*  
        B: *I think it's yours.*



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- complex interactions, e.g. buying a car (cf. Eckardt, draft)

## Worries about lexical equivalence: expers, Effect

- can we always find a suitable lexical paraphrase known to the relevant group?

(10) *I hereby declare you dean of the philosophical faculty.*

compare Putnam's *elms* and *beeches*...

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- Truckenbrodt aims to explain why update amounts to truth, but does not explain why update takes place (invariably)

# Truckenbrodt: a technical problem after all -? (*pace Eckardt*)

Updating  $CB_{A,w}$  with a proposition of the form  $CB_A(\phi)$  seems worrisome. . .

- $CB_A$  does not warrant negative introspection (the corresponding relation need not be euclidian).  
In other words,  $\neg CB_{A,w}(\phi)$  is compatible with  $\neg CB_{A,w}(\neg CB_A(\phi))$ .

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- This is crucial, because Truckenbrodt's approach relies on an update of the context set with a proposition of the form  $CB_{A,w}(\phi)$ .
- Homework: Can we show that a non-trivial update with  $CB_{A,w}(\phi)$  requires belief revision for at least one individual?

# Outline

- 1 Role and interpretation of 'agreement'
- 2 Logic of mutual joint belief (Stalnaker 2002, Fagin & al. 1995)
- 3 Truckenbrodt 2008: self-verification for social act propositions
- 4 Reconsidering social facts**
- 5 Conclusion

# Social facts

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For all worlds, social facts  $\phi$  and relevant groups  $A$  for  $\phi$ :  
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What about  $\phi \rightarrow CB_A(\phi)$ ?

We don't think so (contra Truckenbrodt 2008).

- (11)
- a. *Is this my pencil or yours?*
  - b. *Does the car already belong to us or do we have to sign more papers?*

Special status of social facts w.r.t. mutual agreement is crucial for the automatic update effect observed with explicit performatives. Compare brute facts: *The Eiffeltower is in Berlin..*

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to do:

- 1 goal: work out a weaker version of the special status of institutional facts w.r.t. presumed background information
- 2 reconsider the lexical meaning of social fact-description